

ANALYTIC GEOMETRY IN GRAPHS EXAMPLES

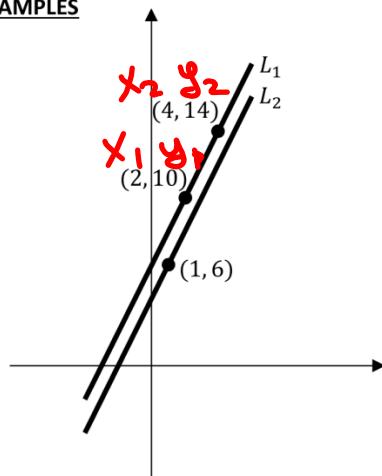
- 1) Line 1 is parallel to Line 2. Find the equation of Line 2.

1) a?

$$\begin{aligned} a &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{14 - 10}{4 - 2} \\ &= \frac{4}{2} \\ &= 2 \end{aligned}$$

2) b?

$$\begin{aligned} y &= 2x + b \\ 6 &= 2(1) + b \\ 6 &= 2 + b \\ b &= 4 \end{aligned}$$



$$y = 2x + 4$$

- 2) Find the x-intercept of Line 1.

1) a?

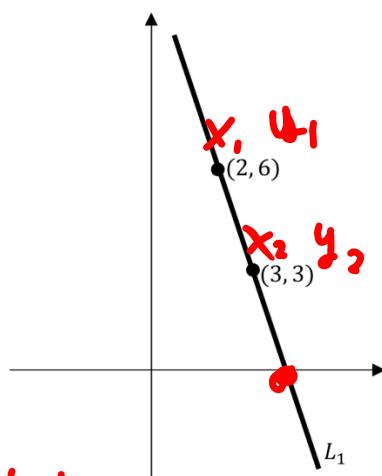
$$a = \frac{3-6}{3-2} = \frac{-3}{1} = -3$$

2) b?

$$\begin{aligned} y &= -3x + b \\ 3 &= -3(3) + b \\ 3 &= -9 + b \\ 3 + 9 &= b \\ b &= 12 \\ y &= -3x + 12 \end{aligned}$$

3) x-int:

$$\begin{aligned} 0 &= -3x + 12 \\ -12 &= -3x \\ \frac{-12}{-3} &= \frac{-3x}{-3} \\ x &= 4 \\ (4, 0) & \end{aligned}$$



- 3) Line 1 is perpendicular to Line 2. Find the distance between A and B.

1) a?

$$a = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{9-7}{10-6}$$

$$= \frac{2}{4}$$

$$= \frac{1}{2} \rightarrow -2$$

2) b?

$$y = -2x + b$$

$$7 = -2(6) + b$$

$$7 = -12 + b$$

$$19 = b$$

$$y = -2x + 19$$

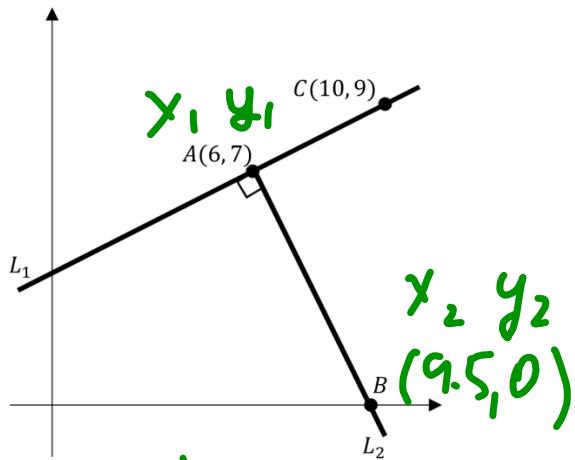
3) B?

$$0 = -2x + 19$$

$$2x = 19$$

$$x = \frac{19}{2} = 9.5$$

$$B(9.5, 0)$$



4) d?

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(9.5 - 6)^2 + (0 - 7)^2}$$

$$= \sqrt{3.5^2 + (-7)^2}$$

$$= \sqrt{12.25 + 49}$$

$$= 7.83 \text{ units}$$

- 4) Find the x-intercept of Line 2.
 - Line 1 is perpendicular to Line 2
 - P is the midpoint of AB

1) a?

$$a = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - 6}{4 - 0} = -2 - 6$$

$$= -2 \rightarrow \frac{1}{2}$$

2) P?

$$P\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$P(2, 2)$$

3) b?

$$y = \frac{1}{2}x + b$$

$$2 = \frac{1}{2}(2) + b$$

$$2 = 1 + b$$

$$b = 1$$

$$y = \frac{1}{2}x + 1$$

4) x-int:

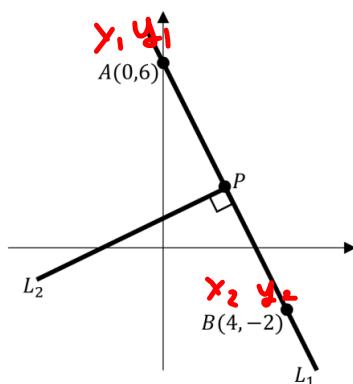
$$0 = \frac{1}{2}x + 1$$

~~$$\frac{-1}{1} = \frac{1x}{2}$$~~

$$1x = -2$$

$$x = -2$$

$$(-2, 0)$$



- 5) A car is travelling along a straight path from $A(-24, -39)$ to $B(30, 33)$. The car breaks down at point C after completing $\frac{2}{3}$ of the trip. A tow truck brings the car to the garage, at point G . How far does the tow truck travel?

SOLUTION1: C ?

$$\begin{aligned}x_p &= x_1 + \frac{a}{b}(x_2 - x_1) = -24 + \frac{2}{3}(30 - -24) \\&= -24 + \frac{2}{3}(54) = -24 + 36 = 12 \\y_p &= y_1 + \frac{a}{b}(y_2 - y_1) = -39 + \frac{2}{3}(33 - -39) \\&= -39 + \frac{2}{3}(72) = -39 + 48 = 9 \\C(12, 9) &\end{aligned}$$

2: a ?

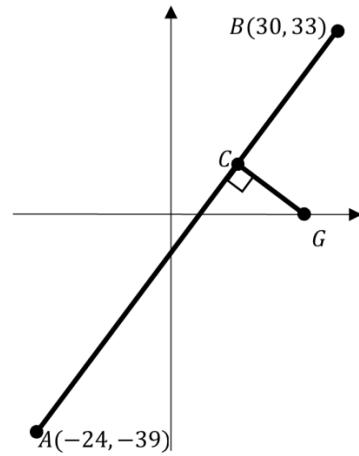
$$a = \frac{y_2 - y_1}{x_2 - x_1} = \frac{33 - -39}{30 - -24} = \frac{72}{54} = \frac{4}{3} \rightarrow -\frac{3}{4}$$

3: b ?

$$\begin{aligned}y &= ax + b \\y &= -\frac{3}{4}x + b \\9 &= -\frac{3}{4}(12) + b \\9 &= -9 + b \\18 &= b \\\therefore y &= -\frac{3}{4}x + 18\end{aligned}$$

4: G (x -intercept)?

$$\begin{aligned}0 &= -\frac{3}{4}x + 18 \\-18 &= -\frac{3}{4}x \\x &= 24 \\G(24, 0) &\end{aligned}$$

5: d_{CG} ?

$$\begin{aligned}d &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\&= \sqrt{(24 - 12)^2 + (0 - 9)^2} \\&= \sqrt{12^2 + (-9)^2} \\&= \sqrt{144 + 81} \\&= \sqrt{225} \\d &= 15 \text{ units}\end{aligned}$$